

You may remove this sheet from the exam. Do not write answers here.

Math facts

For any state function $z(x, y)$ the total differential dz is $dz = \left(\frac{\partial z}{\partial x}\right)_y dx + \left(\frac{\partial z}{\partial y}\right)_x dy$

Euler Reciprocity Theorem (a.k.a. Clairault's theorem).

For any state function $z(x, y)$: $\left(\frac{\partial^2 z}{\partial x \partial y}\right) = \left(\frac{\partial^2 z}{\partial y \partial x}\right)$

Cyclic Rule: $\left(\frac{\partial x}{\partial y}\right)_z \left(\frac{\partial y}{\partial z}\right)_x \left(\frac{\partial z}{\partial x}\right)_y = -1$

Definitions and key equations

Virial equation: $pV_m = RT + Bp + Cp^2 + \dots$ $B(T)$ = second virial coefficient

Work of expansion and compression (pV work): $dw \equiv -p_{\text{ex}}dV$

$dU \equiv dq + dw$

$H \equiv U + pV$

$C_V \equiv (\partial U / \partial T)_V$

$C_p \equiv (\partial H / \partial T)_p$

$\mu_{JT} \equiv (\partial T / \partial p)_H$

$dS \equiv dq_{\text{rev}} / T$

$A \equiv U - TS$

$G \equiv H - TS$

Inequality of Clausius: $(dq - TdS) \leq 0$

For an ideal gas:

$pV = nRT$, $C_p = C_V + nR$, $dU = C_V dT$, $dH = C_p dT$

Isothermal reversible expansion/compression (pV work only): $w = -nRT \ln(V_2/V_1)$

Adiabatic reversible expansion/compression (pV work only):

$V T^{C_V/nR} = \text{constant}$ and $p V^\gamma = \text{constant}$ where $\gamma = C_p/C_V$

Fundamental equations (closed systems, reversible, pV work only):

$dU = +TdS - pdV$

$dH = +TdS + Vdp$

$dA = -SdT - pdV$

$dG = -SdT + Vdp$